# The 2022 ICPC Asia Ho Chi Minh Regional Contest 

HCMUTE - 9 December 2022
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## Problem K K Paths

In graph theory, a tree is a connected undirected graph which does not have any cycles. A tree containing $n$ vertices has exactly $n-1$ edges. For every pair of vertices $(u, v)$ in the tree, there is exactly one simple path between $u$ and $v$. A simple path is a path which passes through each vertex at most once.

You are given a tree containing $n$ vertices. These vertices are numbered from 1 to $n$, inclusive. Let $a_{i}$ be the label of the $i$-th vertex.

You need to select $k$ disjoint simple paths, so that the starting vertex of every path differs from its ending one, and the maximum sum of the labels of the starting and ending vertices of a path is minimized.

Formally, you need to select $k$ pairs of vertices $\left(s_{1}, e_{1}\right),\left(s_{2}, e_{2}\right), \ldots,\left(s_{k}, e_{k}\right)$ satisfying all below conditions:

- For every $i$ such that $1 \leq i \leq k, s_{i} \neq e_{i}$.
- Let's consider $k$ simple paths on the tree: The simple path between $s_{1}$ and $e_{1}$, the simple path between $s_{2}$ and $e_{2}, \ldots$, the simple path between $s_{k}$ and $e_{k}$. These $k$ paths must be pairwise disjoint. In other words, every vertex in the tree belongs to at most one of these $k$ paths.
- The value $\max \left(a_{s_{1}}+a_{e_{1}}, a_{s_{2}}+a_{e_{2}}, \ldots, a_{s_{k}}+a_{e_{k}}\right)$ is as small as possible.


## Input

The first line of the input contains two integers $n$ and $k\left(2 \leq n \leq 10^{5}, 1 \leq k \leq \frac{n}{2}\right)$.
The second line contains $n$ integers: $a_{1}, a_{2}, \ldots, a_{n}\left(0 \leq a_{i} \leq 10^{9}\right)$.
In the last $n-1$ lines, each contains two integers $u$ and $v(1 \leq u, v \leq n)$ indicating that two vertices $u$ and $v$ is directly connected by an edge.

It is guaranteed that the given edges form a tree.

## Output

Print a single integer denoting the minimum possible value of the above expression. If it is impossible to select $k$ pairs of vertices satisfying all the above conditions, print -1 instead.

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## Explanation to samples

In the first sample:


In the second sample:


| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 42 | 2 |
| $10 \quad 20 \quad 30 \quad 40$ | 70 |
| 1 | 2 |
| 2 | 3 |
| 3 | 4 |$\quad$.


| Sample Input 2 | Sample Output 2 |
| :---: | :---: |
| 41 | 30 |
| 10203040 |  |
| 12 |  |
| 13 |  |
| 14 |  |


| Sample Input 3 | Sample Output 3 |
| :---: | :---: |
| 42 | -1 |
| 10203040 |  |
| 12 |  |
| 13 |  |
| 14 |  |

