

The 2022 ICPC Asia Ho Chi Minh Regional Contest

HCMUTE – 9 December 2022



Problem H Hardest Problem

Given two integers n and $d \ (1 \le d \le n)$. Define f(k) as the number of permutations of $1, 2, \ldots, n$ such that:

- the number of inversions of the permutation is k.
- when removing all elements with values that are **strictly** greater than *d* from the permutation, the remaining elements are sorted in increasing order.

Find f(k) modulo 998 244 353 for all k from 1 to min{250 000, $\frac{n \cdot (n-1)}{2}$ }.

A permutation is an array consisting of n distinct integers from 1 to n in arbitrary order. For example, [2, 3, 1, 5, 4] is a permutation, but [1, 2, 2] is not a permutation (2 appears twice in the array) and [1, 3, 4] is also not a permutation (n = 3 but there is 4 in the array).

An inversion of a permutation p is a pair (i, j) $(1 \le i < j \le |p|)$ such that $p_i > p_j$.

Input

The first and only line contains two integers n and d ($2 \le n \le 10^6$, $1 \le d \le n$).

Output

Print min $\{250\ 000, \frac{n \cdot (n-1)}{2}\}$ lines. On the k-th line, print f(k) modulo 998 244 353.

Explanation of the samples

In the first example, n = 2, d = 1. There are two permutations of length 2, that are $\{1, 2\}$ and $\{2, 1\}$. $\{2, 1\}$ is the only permutation that has 1 inversion.

In the second example, n = 5, d = 3.

- For k = 1, there are 2 permutations: $\{\underline{1}, \underline{2}, \underline{3}, 5, 4\}$, $\{\underline{1}, \underline{2}, 4, \underline{3}, 5\}$
- For k = 2, there are 3 permutations: $\{\underline{1}, \underline{2}, 4, 5, \underline{3}\}$, $\{\underline{1}, \underline{2}, 5, \underline{3}, 4\}$, $\{\underline{1}, 4, \underline{2}, \underline{3}, 5\}$
- For k=3, there are 4 permutations: $\{\underline{1},\underline{2},5,4,\underline{3}\}$, $\{\underline{1},4,\underline{2},5,\underline{3}\}$, $\{\underline{1},5,\underline{2},\underline{3},4\}$, $\{4,\underline{1},\underline{2},\underline{3},5\}$
- For k=4, there are 4 permutations: $\{\underline{1},4,5,\underline{2},\underline{3}\}$, $\{\underline{1},5,\underline{2},4,\underline{3}\}$, $\{4,\underline{1},\underline{2},5,\underline{3}\}$, $\{5,\underline{1},\underline{2},\underline{3},4\}$
- For k = 5, there are 3 permutations: $\{\underline{1}, 5, 4, \underline{2}, \underline{3}\}$, $\{4, \underline{1}, 5, \underline{2}, \underline{3}\}$, $\{5, \underline{1}, \underline{2}, 4, \underline{3}\}$
- For k = 6, there are 2 permutations: $\{4, 5, \underline{1}, \underline{2}, \underline{3}\}$, $\{5, \underline{1}, 4, \underline{2}, \underline{3}\}$
- For k = 7, there is 1 permutation: $\{5, 4, \underline{1}, \underline{2}, \underline{3}\}$



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For k = 8, 9 or 10, there are no satisfying permutations.

Sample Input 1	Sample Output 1
2 1	1
Sample Input 2	Sample Output 2
5 3	2
	3
	4
	4
	3
	2
	1
	0
	0
	0