

## The 2022 ICPC Asia Ho Chi Minh Regional Contest

HCMUTE – 9 December 2022



# Problem B Binary Assignment

Vuong is one of the greatest mathematicians of all time! His hobby is to find out mathematical properties of everything, and sometimes even of non-existing things! On his birthday, his programmer friend gave him a binary string S of length n. After a while, he has found out two very interesting properties of S:

- X(S) the length of the **shortest** string that is **not** a *subsequence* of S
- Y(S) the number of the strings that are **not** subsequence of S of length X(S)

Seeing Vuong had fun finding out these two properties, his programmer friend think that it would be great to also change the string S a little bit. The programmer will sequentially do q modifications to the string S. Each modification is one of the following types:

- $0 l r \text{set } S_l, S_{l+1}, \ldots, S_r \text{ to } 0.$
- $1 l r \text{set } S_l, S_{l+1}, \dots, S_r \text{ to } 1.$
- $\mathbb{F} \ l \ r \ -\text{flip} \ S_l, S_{l+1}, \dots, S_r$ . That is, for  $l \le i \le r$ , if  $S_i$  is 0, set it to 1, else set it to 0.

And of course, for each modified version of S, Vuong was also gladly to find X(S) and Y(S), because it was his birthday!

But a puzzle is not complete without an answer. Given the string S and the list of q modifications to the string S, help the programmer friend finding X(S) and Y(S) for each modification, so that he can check Vuong's result with the answer.

Because the answer can be very large, please output the answer modulo  $10^9 + 7$ .

A string a is a subsequence of a string b if a can be obtained from b by deletion of several (possibly, zero or all) characters. For example, "bd", "acd", "b" are subsequences of "abcd", while "da" is not.

#### Input

The first line contains two integers n and q ( $1 \le n, q \le 100\,000$ ) – the length of string S, and the number of modifications.

The second line contains the binary string S of length n.

The *i*-th line on the next q lines contains the description of the *i*-th operation in one of the following forms:

- $0 l r (1 \le l \le r \le n) \text{set } S_l, S_{l+1}, \dots, S_r \text{ to } 0.$
- $1 l r (1 \le l \le r \le n) \text{set } S_l, S_{l+1}, \dots, S_r \text{ to } 1.$
- $F l r (1 \le l \le r \le n) flip S_l, S_{l+1}, \dots, S_r.$



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#### Output

For each modification of S, output on a line two integers X(S) and Y(S) modulo  $10^9 + 7$ .

### **Explanation of the samples**

In the example, the string S is 0110, and there are q = 3 modifications to S. The following table demonstrates the modifications of S.

Order	Modification	Value of $S$	X(S)	Y(S)
Initial		0110	3	5
1	023	0 <u>00</u> 0	1	1
2	134	00 <u>11</u>	2	1
3	F 2 3	0 <u>10</u> 1	3	4

- For S = 0000, X(S) = 1 and Y(S) = 1, because there is one string of length 1 that is **not** a *subsequence* of S, which is the string 1.
- For S = 0.011, the string 10 is the shortest, and is the only string of length 2 that is **not** a subsequence of S.
- For S = 0101, the list of strings of shortest length that are **not** subsequences of S is  $\{000, 100, 110, 111\}$ .
- For the *initial* string S = 0110, the list of strings of shortest length that are **not** subsequences of S is

 $\{000, 001, 100, 101, 111\}$ . So X(S) = 3 and Y(S) = 5, but you don't have to print these numbers.

Sample Input 1	Sample Output 1	
4 3	1 1	
0110	2 1	
0 2 3	3 4	
1 3 4		
F 2 3		