# The 2022 ICPC Asia Ho Chi Minh Regional Contest 

HCMUTE - 9 December 2022
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## Problem B Binary Assignment

Vuong is one of the greatest mathematicians of all time! His hobby is to find out mathematical properties of everything, and sometimes even of non-existing things! On his birthday, his programmer friend gave him a binary string $S$ of length $n$. After a while, he has found out two very interesting properties of $S$ :

- $X(S)$ - the length of the shortest string that is not a subsequence of $S$
- $Y(S)$ - the number of the strings that are not subsequence of $S$ of length $X(S)$

Seeing Vuong had fun finding out these two properties, his programmer friend think that it would be great to also change the string $S$ a little bit. The programmer will sequentially do $q$ modifications to the string $S$. Each modification is one of the following types:

- $0 l r-\operatorname{set} S_{l}, S_{l+1}, \ldots, S_{r}$ to 0 .
- 1 lr $-\operatorname{set} S_{l}, S_{l+1}, \ldots, S_{r}$ to 1 .
- F lr - flip $S_{l}, S_{l+1}, \ldots, S_{r}$. That is, for $l \leq i \leq r$, if $S_{i}$ is 0 , set it to 1 , else set it to 0 .

And of course, for each modified version of $S$, Vuong was also gladly to find $X(S)$ and $Y(S)$, because it was his birthday!

But a puzzle is not complete without an answer. Given the string $S$ and the list of $q$ modifications to the string $S$, help the programmer friend finding $X(S)$ and $Y(S)$ for each modification, so that he can check Vuong's result with the answer.

Because the answer can be very large, please output the answer modulo $10^{9}+7$.
A string $a$ is a subsequence of a string $b$ if $a$ can be obtained from $b$ by deletion of several (possibly, zero or all) characters. For example, "bd", "acd", "b" are subsequences of "abcd", while "da" is not.

## Input

The first line contains two integers $n$ and $q(1 \leq n, q \leq 100000)$ - the length of string $S$, and the number of modifications.

The second line contains the binary string $S$ of length $n$.
The $i$-th line on the next $q$ lines contains the description of the $i$-th operation in one of the following forms:

- $0 \operatorname{lr}(1 \leq l \leq r \leq n)-\operatorname{set} S_{l}, S_{l+1}, \ldots, S_{r}$ to 0 .
- $1 l r(1 \leq l \leq r \leq n)-\operatorname{set} S_{l}, S_{l+1}, \ldots, S_{r}$ to 1 .
- $\operatorname{Flr}(1 \leq l \leq r \leq n)-\operatorname{flip} S_{l}, S_{l+1}, \ldots, S_{r}$.


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## Output

For each modification of $S$, output on a line two integers $X(S)$ and $Y(S)$ modulo $10^{9}+7$.

## Explanation of the samples

In the example, the string $S$ is 0110 , and there are $q=3$ modifications to $S$.
The following table demonstrates the modifications of $S$.

| Order | Modification | Value of $S$ | $X(S)$ | $Y(S)$ |
| :---: | :---: | :---: | :---: | :---: |
| Initial |  | 0110 | 3 | 5 |
| 1 | 023 | $0 \underline{000}$ | 1 | 1 |
| 2 | 134 | 0011 | 2 | 1 |
| 3 | F 23 | $0 \underline{101}$ | 3 | 4 |

- For $S=0000, X(S)=1$ and $Y(S)=1$, because there is one string of length 1 that is not a subsequence of $S$, which is the string 1 .
- For $S=0011$, the string 10 is the shortest, and is the only string of length 2 that is not a subsequence of $S$.
- For $S=0101$, the list of strings of shortest length that are not subsequences of $S$ is $\{000,100,110,111\}$.
- For the initial string $S=0110$, the list of strings of shortest length that are not subsequences of $S$ is
$\{000,001,100,101,111\}$. So $X(S)=3$ and $Y(S)=5$, but you don't have to print these numbers.

| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 4 | 3 |
| 0 | 110 |
| 0 | 2 |
| 1 | 3 | 4

