

## **Problem E: Birthday Cake**

Time limit: 1s; Memory limit: 256 MB

Bob is celebrating his birthday with his friends. During the party, Bob wants to cut the birthday cake and share it with his friends.

The birthday cake is a rectangle of size R x C made from a variety of materials. Let a[i][j] is the calories of the cell in *i*-th row and *j*-th column, total calories of a piece of cake are the sum of its cells.

There are *n* friends in the party. Because of the fear of obesity, they do not want to eat too much. Let p[k] is the maximum calories of *k*-th friend.

Bob wants to cut this cake n - 1 times to obtain n smaller pieces which can be given to their friends. Bob must cut exactly n - 1 times, according to the following rule:

- During the *l*-th cut, Bob must cut the current (rectangular) piece of cake horizontally or vertically so that it results in two 2 smaller (rectangular) pieces, each piece must be of size at least 1×1.
  - If the *l*-th cut was done horizontally, the upper piece must be given to the *l*-th friend, and the lower piece of cake must be used for the next cutting phase.
  - If the *l*-th cut was done vertically, the left piece must be given to the *l*-th friend, and the right piece of cake must be used for the next cutting phase.
- After n 1 cuts, there are exactly n pieces of cake to be given to n friends with no leftovers. The *l*-th piece of cake must satisfy the *l*-th friend's calorie condition, that is, total calories of the *i*-th piece of cake must not be greater than p[*l*].

For example: let n = 3, p = [5, 10, 15] and the below birthday cake:

1	5
2	8



Method 1:	Before the horizontal cut		Before the	ne vertical cut	The total calories of the	
	1	5		2	8	pieces of cake are $[6, 2, 8]$ . The first piece is not satisfied due to $6 > 5$ .
	2	8		After		
	After			2 8		
	1	5				
	2	8				
Method 2:	Before the vertical cut		Before the	Before the horizontal cut	The total calories of the	
	1	5		5		pieces are [3, 5, 8] satisfying for n friends.
	2	8		8		
	After			After		
	1	5		5		
	2	8		8		

Given the calories of the cake and the maximum calories of n friends, please help Bob compute the number of different ways to cut the cake that meet all rules and satisfy all friends.

## Input

The first line contains 3 integers R, C, and *n*.  $(1 \le R, C \le 100, 1 \le n \le min(10, R + C - 1))$ .

The next R lines, each line contains C numbers, that is the calorie of the cell a[i][j].  $(0 \le a[i][j] \le 100)$ .

The next line contains *n* integers, the *i*-th integer is the maximum calories p[k] of the *k*-th friend.  $(0 \le p[k] \le 10^6)$ .



## Output

Output the number of different ways to cut the cake that meet all rules and satisfy

all friends. Since the answer can be quite large, output the answer module  $10^9+7$ .

## Sample

Input	Output
223	1
15	
28	
5 10 15	
332	3
10 8 6	
8410	
110	
78 25	