## Problem E: Birthday Cake

Time limit: 1s; Memory limit: 256 MB

Bob is celebrating his birthday with his friends. During the party, Bob wants to cut the birthday cake and share it with his friends.
The birthday cake is a rectangle of size $\mathrm{R} \times \mathrm{C}$ made from a variety of materials. Let $\mathrm{a}[i][j]$ is the calories of the cell in $i$-th row and $j$-th column, total calories of a piece of cake are the sum of its cells.
There are $n$ friends in the party. Because of the fear of obesity, they do not want to eat too much. Let $\mathrm{p}[k]$ is the maximum calories of $k$-th friend.
Bob wants to cut this cake $n-1$ times to obtain $n$ smaller pieces which can be given to their friends. Bob must cut exactly $n-1$ times, according to the following rule:
$>$ During the $l$-th cut, Bob must cut the current (rectangular) piece of cake horizontally or vertically so that it results in two 2 smaller (rectangular) pieces, each piece must be of size at least $1 \times 1$.

- If the $l$-th cut was done horizontally, the upper piece must be given to the $l$-th friend, and the lower piece of cake must be used for the next cutting phase.
- If the $l$-th cut was done vertically, the left piece must be given to the $l$-th friend, and the right piece of cake must be used for the next cutting phase.
$>$ After $n-1$ cuts, there are exactly $n$ pieces of cake to be given to $n$ friends with no leftovers. The $l$-th piece of cake must satisfy the $l$-th friend's calorie condition, that is, total calories of the $i$-th piece of cake must not be greater than $\mathrm{p}[l]$.

For example: let $n=3, \mathrm{p}=[5,10,15]$ and the below birthday cake:

| 1 | 5 |
| :---: | :---: |
| 2 | 8 |


| Method 1: | Before the horizontal cut |  | Before the vertical cut |  | The total calories of the pieces of cake are $[6,2,8]$. The first piece is not satisfied due to $6>5$. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | $5$ | $2$ | $8$ |  |
|  | 2 | 8 |  |  |  |
|  | After |  | 2 | 8 |  |
|  | 1 | 5 |  |  |  |
|  | 2 | 8 |  |  |  |
| Method 2: | Before the vertical cut |  | Before the horizontal cut |  | The total calories of the pieces are $[3,5,8]$ satisfying for n friends. |
|  | 1 | 5 | 5 |  |  |
|  | 2 | 8 | 8 |  |  |
|  | After |  | After |  |  |
|  | 1 | 5 | 5 |  |  |
|  | 2 | 8 |  |  |  |
|  |  | , | 8 |  |  |

Given the calories of the cake and the maximum calories of n friends, please help Bob compute the number of different ways to cut the cake that meet all rules and satisfy all friends.

## Input

The first line contains 3 integers $\mathrm{R}, \mathrm{C}$, and $n .(1 \leq \mathrm{R}, \mathrm{C} \leq 100,1 \leq \mathrm{n} \leq \min (10, \mathrm{R}+$ $\mathrm{C}-1)$ ).

The next R lines, each line contains C numbers, that is the calorie of the cell $\mathrm{a}[i][j]$. ( $0 \leq \mathrm{a}[i][j] \leq 100$ ).

The next line contains $n$ integers, the $i$-th integer is the maximum calories $\mathrm{p}[k]$ of the $k$-th friend. $\left(0 \leq \mathrm{p}[k] \leq 10^{6}\right)$.

## Output

Output the number of different ways to cut the cake that meet all rules and satisfy all friends. Since the answer can be quite large, output the answer module $10^{9}+7$.

## Sample

| Input | Output |
| :--- | :--- |
| 223 | 1 |
| 15 |  |
| 28 |  |
| 51015 | 3 |
| 332 |  |
| 1086 |  |
| 8410 |  |
| 110 |  |
| 7825 |  |

