

## BITSEQ

You're given two sequences of  $n$  nonnegative integer numbers:  $a_1, a_2, \dots, a_n$  and  $c_1, c_2, \dots, c_n$ . The sequence of  $m$  integer numbers  $i_1, i_2, \dots, i_m$  is called *beautiful* if it meets with the following criteria:

- $1 \leq i_1 < i_2 < \dots < i_m \leq n$ . In other words, sequence must be increasing.
- $\text{cntbit}(a_{i_{j-1}} \text{ AND } a_{i_j}) = c_{i_j}$  for all  $1 < j \leq m$ .

Find longest *beautiful* sequence.

### Note

$\text{cntbit}(x)$  — number of ones in binary representation  $x$ , e.g.  $\text{cntbit}(5_{10}) = \text{cntbit}(101_2) = 2$ ,  $\text{cntbit}(0) = 0$ ,  $\text{cntbit}(8) = 1$ .

*AND* — is a binary operation, which takes two equal-length binary representations and performs the logical *AND* operation on each pair of the corresponding bits, e.g.  $11_{10} \text{ AND } 13_{10} = 1011_2$  AND  $1101_2 = 1001_2 = 9$ ,  $7_{10} \text{ AND } 16_{10} = 111_2$  AND  $10000_2 = 0_2 = 0_10$ .

### Implementation Details

```
int[] bitseq(int[] a, int[] c)
```

- $a, c$ : arrays of length  $n$ .

### Constraints

- $1 \leq n \leq 10^5$
- $0 \leq a_i < 2^{20}$
- $0 \leq c_i \leq 20$

### Examples

#### Example 1

Analyze this function call:

```
int[] bitseq(4, [1, 2, 3, 4], [2, 0, 1, 0])
```

The sequence  $a$  from the input is itself a *beautiful* sequence because:

- $\text{cntbit}(a_1 \text{ AND } a_2) = \text{cntbit}(1_{10} \text{ AND } 2_{10}) = \text{cntbit}(001_2 \text{ AND } 010_2) = 0 = c_2$
  - $\text{cntbit}(a_2 \text{ AND } a_3) = \text{cntbit}(2_{10} \text{ AND } 3_{10}) = \text{cntbit}(010_2 \text{ AND } 011_2) = 1 = c_3$
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- $\text{cntbit}(a_3 \text{ AND } a_4) = \text{cntbit}(3_{10} \text{ AND } 4_{10}) = \text{cntbit}(011_2 \text{ AND } 100_2) = 0 = c_4$

Therefore, the resulting longest *beautiful* sequence is the sequence  $a$  itself,  $[1, 2, 3, 4]$ .

## Example 2

Analyze this function call:

```
int[] bitseq(5, [9, 7, 9, 7, 9], [3, 1, 4, 1, 4])
```

The resulting longest *beautiful* sequence are sequences  $[1, 2]$  and  $[1, 4]$ , any of the two solutions is valid.

## Subtasks

1. (7 points):  $1 \leq n \leq 15, 0 \leq a_i < 2^{20}$
2. (16 points):  $1 \leq n \leq 5000, 0 \leq a_i < 2^{20}$
3. (17 points):  $1 \leq n \leq 10^5, 0 \leq a_i < 2^8$
4. (60 points): No additional constraints.

## Sample Grader

The sample grader reads in the input in the following format:

- line 1:  $n$
- line 2:  $a_1 a_2 \dots a_n$
- line 3:  $c_1 c_2 \dots c_n$

The sample grader prints your answers in the following format:

- line 1: Length of the longest *beautiful* sequence.
  - line 2: The longest sequence returned from `bitseq`.
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