

# TRAFFIC

The city of Free Contest has a **circular structure**, with  $n$  intersections numbered 1 to  $n$  clockwise. The city also has  $n$  roads placed on the perimeter of the city, with the  $i$ -th road connecting the  $i$ -th intersection to the  $(i \bmod n)+1$ -th intersection and taking  $w_i$  seconds to travel through.

Due to the inefficiency of the traffic system,  $m$  more roads are built. The  $j$ -th new road is built on a straight line, connects the intersection  $a_j$  with the intersection  $b_j$ , and takes  $c_j$  seconds to travel through. All the  $n + m$  roads do not intersect with each other, except at the two endpoints of the road (which are among the  $n$  intersections).

Currently, the city is calculating **the efficiency of the new travelling system**. Let the function  $d(x, y)$  be the shortest amount of time to travel between the  $x$ -th intersection and the  $y$ -th intersection. The efficiency of the traffic system is equal to  $\sum_{x=1}^{n-1} \sum_{y=x+1}^n d(x, y)$ .

Because **the efficiency of the new travelling system** may be large, you only need to output the answer **modulo**  $10^9 + 7$ .

## Implementation Details

```
int traffic(int n, int m, int[] w, int[] a, int[] b, int[] c)
```

- $n$ : the number of intersections.
- $m$ : the number of new roads.
- $w$ : an array of length  $n$  describing the time to travel on the  $n$  pre-existing roads.
- $a, b, c$ : arrays of length  $m$ . With each  $j$  ( $1 \leq j \leq m$ ) describing the  $j$ -th road.

## Constraints

- $3 \leq n \leq 100000$
- $0 \leq m \leq 200000$
- $1 \leq w_i \leq 10^9$
- $1 \leq a_j < b_j \leq N$
- $1 \leq c_j \leq 10^9$

## Examples

### Example 1:

Analyze this function call:

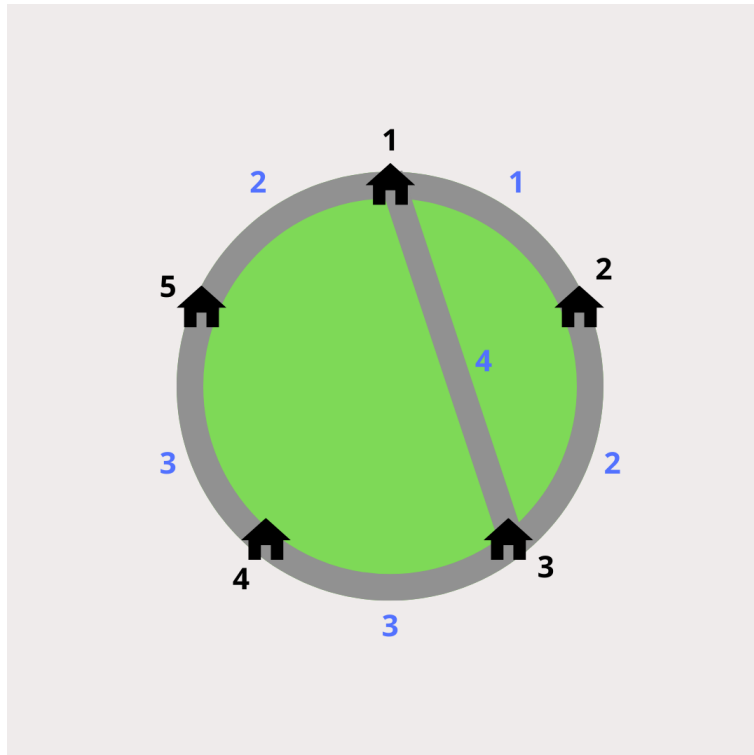
```
int traffic(5, 1, [1, 2, 3, 3, 2], [1], [3], [4])
```

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# IOI Practice Contest 2022

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This is the visualization of the Free Contest city based on the test given above (The intersections (houses) were numbered to make it easier to read):



As such, we can see that the shortest time to travel between the intersections (houses) are:

- $d(1, 2) = 1$ ;  $d(1, 3) = 3$ ;  $d(1, 4) = 5$ ;  $d(1, 5) = 2$ ;
- $d(2, 3) = 2$ ;  $d(2, 4) = 5$ ;  $d(2, 5) = 3$ ;
- $d(3, 4) = 3$ ;  $d(3, 5) = 5$ ;
- $d(4, 5) = 3$ ;

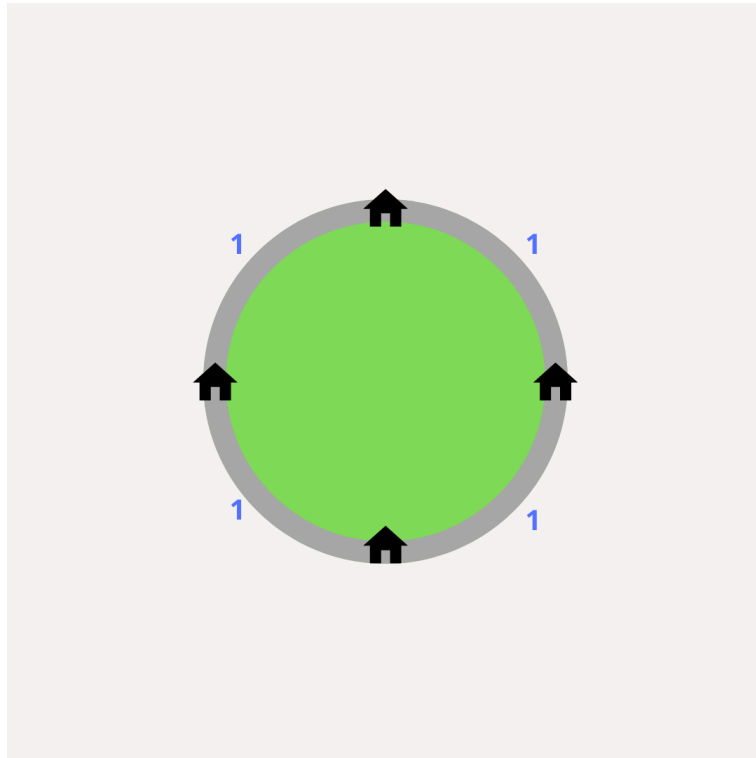
## Example 2:

Analyze this function call:

```
int traffic(4, 0, [1, 1, 1, 1], [], [], [])
```

This is the visualization of the Free Contest city based on the test given above (The intersections (houses) were numbered to make it easier to read):

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## Subtasks

1. (10 points):  $3 \leq n \leq 500$
2. (10 points):  $3 \leq n \leq 2000$
3. (10 points):  $m = 0$
4. (20 points):  $m = 1$
5. (50 points): No extra restriction.

## Sample Graders

The input will be formatted as such:

- line 1:  $n \ m$
- line 2:  $w_0 \ w_1 \ \dots \ w_n$
- line  $3 + j$  ( $1 \leq j \leq m$ ):  $a_j \ b_j \ c_j$

The output will be formatted as such:

- line 1: The return value of the function `traffic`.
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